

ELECTRICITY

Properties of charge (Q) → SI unit - Coulomb (C)

1. Unlike charges attract, like charges repel
2. Charge is additive (Total charge = sum of all charges)

3. $F \propto \frac{q_1 q_2}{r^2}$ Coulomb's law

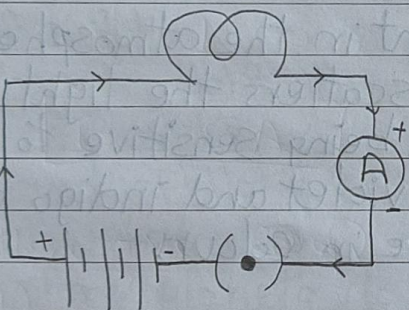
(not in syllabus)

4. Charge is conserved (neither created, nor destroyed)
5. Charge is quantised

$$Q = ne \quad \text{where } e = \text{charge on electron} \\ (1.6 \times 10^{-19} \text{ C}) \\ n = \text{no. of electrons}$$

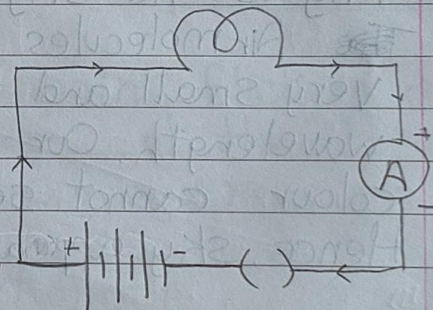
Electric Circuit (ckt)

» Closed and continuous path of the electric current is called electric circuit.



(A)

closed circuit



(B)

open circuit

Electric Current (I)

» Rate of flow of electric charges

$$I = \frac{Q}{t}, \quad Q = It$$

SI unit - Ampere (A)

1 Ampere = $\frac{1 \text{ Coulomb}}{1 \text{ Second}}$

$1 \text{ A} = \frac{1 \text{ C}}{1 \text{ s}}$

$\frac{\text{A} \cdot \text{s}}{\text{C}}$

1 Coulomb = 1 Ampere x 1 second

$1 \text{ C} = 1 \text{ A} \times 1 \text{ s}$

$1 \text{ mA} = 10^{-3} \text{ A}$
milli Ampere

$1 \mu\text{A} = 10^{-6} \text{ A}$
micro Ampere

Q

Calculate the no. of electrons in 1 Coulomb of charge.
 $Q = ne$ $Q = 1 \text{ C}$

$$n = \frac{Q}{e} = \frac{1 \text{ C}}{1.6 \times 10^{-19} \text{ C}} = \frac{0.625}{16 \times 10^{-19}} = \frac{0.625 \text{ C}}{10^{-19} \text{ C}}$$

$$= 0.625 \times 10^{19}$$

$$\rightarrow = \underline{\underline{6.25 \times 10^{18} \text{ electrons}}}$$

Electric Potential and Potential difference

Electric Potential - The electric potential energy per unit charge

Electric Potential difference - The electric potential difference

Potential difference is the amount of work done per unit charge.

Work = (Force x Displacement)
(acts on electrons) → (electrons displace)

$V = \frac{W}{Q}$

Potential difference = $\frac{\text{Work}}{\text{Charge}}$

Ohm's Law

SI unit - Ω

$$V \propto I$$

$I \uparrow - V \uparrow$ (directly proportional)
 $I \downarrow - V \downarrow$

$$V \propto I$$

$$V = IR$$

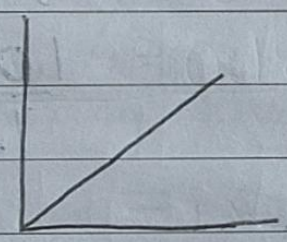
Where V is potential difference
 I is current
 R is Resistance (constant)
oppose electron flow

$$R = \frac{V}{I}$$

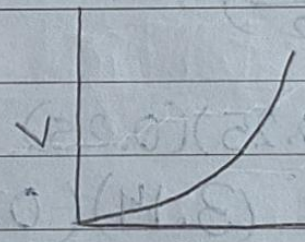
$$I = \frac{V}{R}$$

$R \uparrow - I \downarrow$ (inversely proportional)
 $R \downarrow - I \uparrow$

At constant temperatures, the strength of the current flow is directly proportional to the potential difference across its ends.



Ohmic



Non-ohmic

Resistance depends on:

FACTORS

1. Length of the conductor $L \downarrow, R \downarrow$

① $\leftarrow R \propto L$ (directly proportional) $L \uparrow, R \uparrow$

2. Area of cross section

② $\leftarrow R \propto \frac{1}{A}$ (inversely proportional) $A \uparrow, R \downarrow$
 $A \downarrow, R \uparrow$

3. Nature of material

Metals - $R \downarrow$ (less)

(Alloys) Insulators - $R \uparrow$ (more)

4. Temperature $\propto R$ (Directly Proportional)

Temp. $\uparrow, R \uparrow$

Temp. $\downarrow, R \downarrow$

From ① and ②,

$$R \propto \frac{L}{A}$$

or

$$R = \frac{\rho L}{A}$$

$$\rho = \frac{RA}{L}$$

"Resistivity"

ρ -

ρ (rho) is a constant of proportionality and is called resistivity.

SI unit - $\underline{\underline{\Omega m}}$ $\left[\rho = \frac{RA}{L} = \frac{\Omega m^2}{m} = \underline{\underline{\Omega m}} \right]$

Resistivity = Resistance

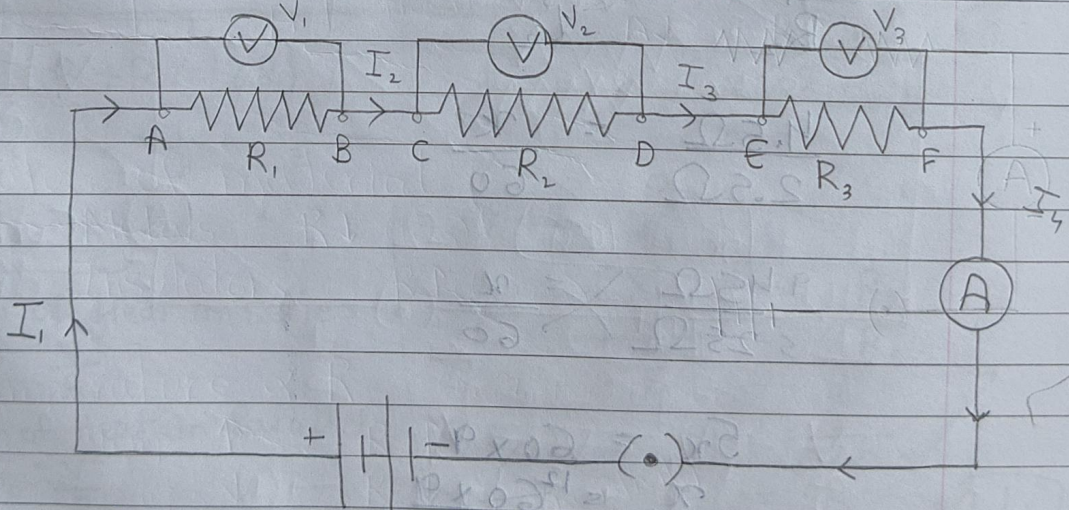
Property of the material which is defined as resistance of the material in particular dimensions of length 1m and area of cross section 1m².

Note: As long as nature of the material changes, resistivity will not change.

[Material change = Resistivity change]
[Material no change = Resistivity no change]

Combination of Resistors

Series combination of Resistors



Current is constant, Voltage is distributed

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$$I_1 = I_2 = I_3 = I_4 \text{ (constant)}$$

$$V = V_1 + V_2 + V_3 \rightarrow \textcircled{1}$$

According to ohm's law

$$V = IR$$

$$\therefore V_1 = IR_1 \rightarrow \textcircled{2}$$

$$V_2 = IR_2 \rightarrow \textcircled{3}$$

$$V_3 = IR_3 \rightarrow \textcircled{4}$$

Substitute eqⁿ ②, ③, ④ in ①

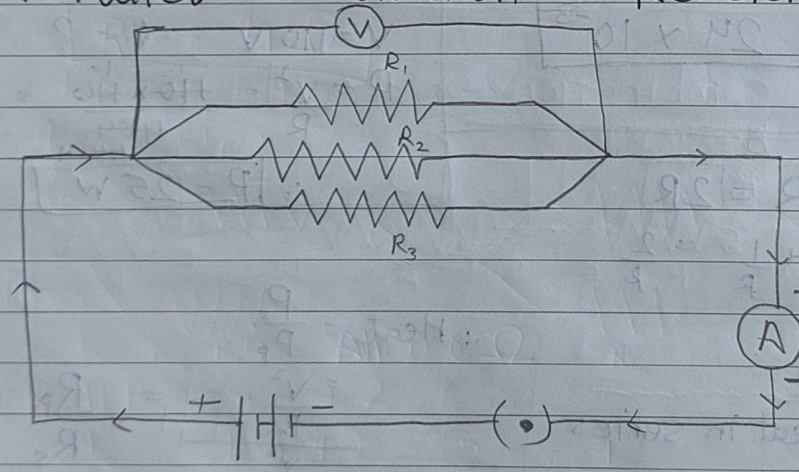
$$IR = IR_1 + IR_2 + IR_3$$

$$R = R_1 + R_2 + R_3$$

$$R_s = R_1 + R_2 + R_3$$

R ↑ I ↓

Parallel Combination of Resistors



Voltage is constant

Current is distributed

$$V = V_1 = V_2 = V_3$$

$$I = I_1 + I_2 + I_3 \rightarrow \textcircled{1}$$

According to Ohm's law

$$V = IR, \quad \left| I = \frac{V}{R} \right|$$

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$$I_1 = \frac{V}{R_1} \rightarrow \textcircled{2}$$

$$I_2 = \frac{V}{R_2} \rightarrow \textcircled{3}$$

$$I_3 = \frac{V}{R_3} \rightarrow \textcircled{4}$$

Substitute eqⁿ $\textcircled{2}$, $\textcircled{3}$, $\textcircled{4}$ in $\textcircled{1}$

$$\frac{V}{R} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$

$$V \left(\frac{1}{R} \right) = V \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)$$

$$\boxed{\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

$$\boxed{R_p = \frac{R}{n}}$$

where n is the number of resistors

HEATING EFFECT OF ELECTRIC CURRENT

1. Whenever a current is passed through a conductor; it becomes hot after some time, which means that the electric energy is converted into heat energy.
2. When we apply potential difference across the ends of the conductor, electrons begin to drift from lower potential to higher potential.
3. The motion of these electrons is not smooth because they experience resistance on account of their collision

$$\boxed{H = I^2 R t} \rightarrow \text{Joule's law of heating}$$

(work) $W = H$

$$\boxed{H = VQ} \quad \left[V = \frac{W}{Q} \Rightarrow W = VQ \right]$$

$$\boxed{H = VIt} \quad [Q = It]$$

$$H = IR \times It \quad [V = IR]$$

$$\boxed{H = I^2 R t}$$

$$H = \left(\frac{V}{R}\right)^2 R t \quad \left[V = IR \Rightarrow I = \frac{V}{R} \right]$$

$$H = \frac{V^2}{R} \times R t$$

$$\boxed{H = \frac{V^2}{R} \cdot t}$$

Applications

1. Iron box
2. Electric heater
3. Toaster
4. Hair dryer
5. Oven
6. Electric bulb
7. Electric fuse